Diploma Programme
Programme du diplôme
Programa del Diploma

Markscheme

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Mathematics: analysis and approaches

Standard level

Paper 2

23 pages

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Instructions to Examiners

Abbreviations

M Marks awarded for attempting to use a correct **Method**.

A Marks awarded for an **Answer** or for **Accuracy**; often dependent on preceding ***M*** marks.

R Marks awarded for clear **Reasoning**.

AG Answer given in the question and so no marks are awarded.

FT Follow through. The practice of awarding marks, despite candidate errors in previous parts, for their correct methods/answers using incorrect results.

Using the markscheme

1 General

Award marks using the annotations as noted in the markscheme *eg* ***M1***, ***A2***.

2 Method and Answer/Accuracy marks

- Do **not** automatically award full marks for a correct answer; all working **must** be checked, and marks awarded according to the markscheme.
- It is generally not possible to award ***M0*** followed by ***A1***, as ***A*** mark(s) depend on the preceding ***M*** mark(s), if any.
- Where ***M*** and ***A*** marks are noted on the same line, *e.g.* ***M1A1***, this usually means ***M1*** for an **attempt** to use an appropriate method (*e.g.* substitution into a formula) and ***A1*** for using the **correct** values.
- Where there are two or more ***A*** marks on the same line, they may be awarded independently; so if the first value is incorrect, but the next two are correct, award ***A0A1A1***.
- Where the markscheme specifies ***A3***, ***M2*** *etc*., do **not** split the marks, unless there is a note.
- The response to a "show that" question does not need to restate the ***AG*** line, unless a **Note** makes this explicit in the markscheme.
- Once a correct answer to a question or part question is seen, ignore further working even if this working is incorrect and/or suggests a misunderstanding of the question. This will encourage a uniform approach to marking, with less examiner discretion. Although some candidates may be advantaged for that specific question item, it is likely that these candidates will lose marks elsewhere too.
- An exception to the previous rule is when an incorrect answer from further working is used **in a subsequent part**. For example, when a correct exact value is followed by an incorrect decimal approximation in the first part and this approximation is then used in the second part. In this situation, award ***FT*** marks as appropriate but do not award the final ***A1*** in the first part.

Examples:

	Correct answer seen	Further working seen	Any FT issues?	Action
1.	$8\sqrt{2}$	5.65685... *(incorrect decimal value)*	No. Last part in question.	Award ***A1*** for the final mark *(condone the incorrect further working)*
2.	$\frac{35}{72}$	$0.468111\ldots$ (incorrect decimal value)	Yes. Value is used in subsequent parts.	Award ***A0*** for the final mark *(and full **FT** is available in subsequent parts)*

3 Implied marks

Implied marks appear in **brackets e.g. *(M1)***,and can only be awarded if **correct** work is seen or implied by subsequent working/answer.

4 Follow through marks (only applied after an error is made)

Follow through (***FT***) marks are awarded where an incorrect answer from one **part** of a question is used correctly in **subsequent** part(s) (e.g. incorrect value from part (a) used in part (d) or incorrect value from part (c)(i) used in part (c)(ii)). Usually, to award ***FT*** marks, **there must be working present** and not just a final answer based on an incorrect answer to a previous part. However, if all the marks awarded in a subsequent part are for the answer or are implied, then ***FT*** marks should be awarded for *their* correct answer, even when working is not present.

For example: following an incorrect answer to part (a) that is used in subsequent parts, where the markscheme for the subsequent part is ***(M1)A1***, it is possible to award full marks for *their* correct answer, **without working being seen.** For longer questions where all but the answer marks are implied this rule applies but may be overwritten by a **Note** in the Markscheme.

- Within a question part, once an **error** is made, no further ***A*** marks can be awarded for work which uses the error, but ***M*** marks may be awarded if appropriate.

- If the question becomes much simpler because of an error then use discretion to award fewer ***FT*** marks, by reflecting on what each mark is for and how that maps to the simplified version.

- If the error leads to an inappropriate value (*e.g.* probability greater than 1, $\sin\theta = 1.5$, non-integer value where integer required), do not award the mark(s) for the final answer(s).

- The markscheme may use the word “their” in a description, to indicate that candidates may be using an incorrect value.

- If the candidate’s answer to the initial question clearly contradicts information given in the question, it is not appropriate to award any ***FT*** marks in the subsequent parts. This

includes when candidates fail to complete a “show that” question correctly, and then in subsequent parts use their incorrect answer rather than the given value.

- Exceptions to these ***FT*** rules will be explicitly noted on the markscheme.

- If a candidate makes an error in one part but gets the correct answer(s) to subsequent part(s), award marks as appropriate, unless the command term was “Hence”.

5 Mis-read

If a candidate incorrectly copies values or information from the question, this is a mis-read (***MR***). A candidate should be penalized only once for a particular misread. Use the ***MR*** stamp to indicate that this has been a misread and do not award the first mark, even if this is an ***M*** mark, but award all others as appropriate.

- If the question becomes much simpler because of the ***MR***, then use discretion to award fewer marks.

- If the ***MR*** leads to an inappropriate value (*e.g.* probability greater than 1, $\sin\theta = 1.5$, non-integer value where integer required), do not award the mark(s) for the final answer(s).

- Miscopying of candidates’ own work does **not** constitute a misread, it is an error.

- If a candidate uses a correct answer, to a “show that” question, to a higher degree of accuracy than given in the question, this is NOT a misread and full marks may be scored in the subsequent part.

- ***MR*** can only be applied when work is seen. For calculator questions with no working and incorrect answers, examiners should **not** infer that values were read incorrectly.

6 Alternative methods

Candidates will sometimes use methods other than those in the markscheme. Unless the question specifies a method, other correct methods should be marked in line with the markscheme. If the command term is ‘Hence’ and not ‘Hence or otherwise’ then alternative methods are not permitted unless covered by a note in the mark scheme.

- Alternative methods for complete questions are indicated by **METHOD 1**, **METHOD 2**, *etc*.
- Alternative solutions for parts of questions are indicated by **EITHER** . . . **OR**.

7 Alternative forms

Unless the question specifies otherwise, **accept** equivalent forms.

- As this is an international examination, accept all alternative forms of **notation** for example 1.9 and $1{,}9$ or 1000 and $1{,}000$ and 1.000.

- Do not accept final answers written using calculator notation. However, ***M*** marks and intermediate ***A*** marks can be scored, when presented using calculator notation, provided the evidence clearly reflects the demand of the mark.

- In the markscheme, equivalent **numerical** and **algebraic** forms will generally be written in brackets immediately following the answer.

- In the markscheme, some **equivalent** answers will generally appear in brackets. Not all equivalent notations/answers/methods will be presented in the markscheme and examiners are asked to apply appropriate discretion to judge if the candidate work is equivalent.

8 Format and accuracy of answers

If the level of accuracy is specified in the question, a mark will be linked to giving the answer to the required accuracy. If the level of accuracy is not stated in the question, the general rule applies to final answers: *unless otherwise stated in the question all numerical answers must be given exactly or correct to three significant figures.*

Where values are used in subsequent parts, the markscheme will generally use the exact value, however candidates may also use the correct answer to 3 sf in subsequent parts. The markscheme will often explicitly include the subsequent values that come "*from the use of 3 sf values*".

Simplification of final answers: Candidates are advised to give final answers using good mathematical form. In general, for an ***A*** mark to be awarded, arithmetic should be completed, and any values that lead to integers should be simplified; for example, $\sqrt{\frac{25}{4}}$ should be written as $\frac{5}{2}$. An exception to this is simplifying fractions, where lowest form is not required (although the numerator and the denominator must be integers); for example, $\frac{10}{4}$ may be left in this form or written as $\frac{5}{2}$. However, $\frac{10}{5}$ should be written as 2, as it simplifies to an integer.

Algebraic expressions should be simplified by completing any operations such as addition and multiplication, e.g. $4e^{2x} \times e^{3x}$ should be simplified to $4e^{5x}$, and $4e^{2x} \times e^{3x} - e^{4x} \times e^{x}$ should be simplified to $3e^{5x}$. Unless specified in the question, expressions do not need to be factorized, nor do factorized expressions need to be expanded, so $x(x+1)$ and $x^2 + x$ are both acceptable.

Please note: intermediate ***A*** marks do NOT need to be simplified.

9 Calculators

A GDC is required for this paper, but If you see work that suggests a candidate has used any calculator not approved for IB DP examinations (eg CAS enabled devices), please follow the procedures for malpractice.

10. Presentation of candidate work

Crossed out work: If a candidate has drawn a line through work on their examination script, or in some other way crossed out their work, do not award any marks for that work unless an explicit note from the candidate indicates that they would like the work to be marked.

More than one solution: Where a candidate offers two or more different answers to the same question, an examiner should only mark the first response unless the candidate indicates otherwise. If the layout of the responses makes it difficult to judge, examiners should apply appropriate discretion to judge which is “first”.

Section A

1. (a) **EITHER**

uses the cosine rule ***(M1)***

$\mathrm{AB}^2 = 5^2 + 5^2 - 2\times5\times5\times\cos1.9$ ***(A1)***

OR

uses right-angled trigonometry ***(M1)***

$\dfrac{\frac{\mathrm{AB}}{2}}{5} = \sin 0.95$ ***(A1)***

OR

uses the sine rule ***(M1)***

$\alpha = \frac{1}{2}(\pi - 1.9)(= 0.6207...)$

$\dfrac{\mathrm{AB}}{\sin 1.9} = \dfrac{5}{\sin 0.6207...}$ ***(A1)***

THEN

$\mathrm{AB} = 8.13415...$

$\mathrm{AB} = 8.13$ (m) ***A1***

[3 marks]

continued…

Question 1 continued

(b) let the shaded area be A

METHOD 1

attempt at finding reflex angle ***(M1)***

$\mathrm{A\hat{O}B} = 2\pi - 1.9 \ (= 4.3831...)$

substitution into area formula ***(A1)***

$A = \frac{1}{2} \times 5^2 \times 4.3831...$ OR $\left(\frac{2\pi - 1.9}{2\pi}\right) \times \pi\left(5^2\right)$

$= 54.7898...$

$= 54.8$ (m²) ***A1***

METHOD 2

let the area of the circle be A_C and the area of the unshaded sector be A_U

$A = A_C - A_U$ ***(M1)***

$A = \pi \times 5^2 - \frac{1}{2} \times 5^2 \times 1.9 \ (= 78.5398... - 23.75)$ ***(A1)***

$= 54.7898...$

$= 54.8$ (m²) ***A1***

[3 marks]

Total [6 marks]

2. METHOD 1

recognises that $g(x) = \int \left(3x^2 + 5e^x\right) \, dx$ ***(M1)***

$g(x) = x^3 + 5e^x \left(+C\right)$ ***(A1)(A1)***

Note: Award ***A1*** for each integrated term.

substitutes $x = 0$ and $y = 4$ into their integrated function (must involve $+C$) ***(M1)***

$4 = 0 + 5 + C \Rightarrow C = -1$

$g(x) = x^3 + 5e^x - 1$ ***A1***

METHOD 2

attempts to write both sides in the form of a definite integral ***(M1)***

$\int_0^x g'(t) \, dt = \int_0^x \left(3t^2 + 5e^t\right) \, dt$ ***(A1)***

$g(x) - 4 = x^3 + 5e^x - 5e^0$ ***(A1)(A1)***

Note: Award ***A1*** for $g(x) - 4$ and ***A1*** for $x^3 + 5e^x - 5e^0$.

$g(x) = x^3 + 5e^x - 1$ ***A1***

[5 marks]

3. (a) **METHOD 1**

using geometric sequence with $r = 1.02$ ***(M1)***

correct expression or listing terms correctly ***(A1)***

45000×1.02^{10} OR $45000 \times 1.02^{11-1}$ OR listing terms

Gemma's salary is \$54855 (must be to the nearest dollar) ***A1***

[3 marks]

METHOD 2

$N = 10$

$\text{PV} = \mp 45000$

$\text{I\%} = 2$

$\text{P/Y} = 1$

$\text{C/Y} = 1$

$FV = \pm 54854.7489...$ ***(M1)(A1)***

Gemma's salary is \$54855 (must be to the nearest dollar) ***A1***

[3 marks]

(b) finds $a = 1096.89...$ and $b = -2160753.8...$ (accept $b = -2.16 \times 10^6$) ***(A1)(A1)***

Note: Award ***(A1)(A1)*** for $S = 1096.89...x + 33028.49...$, or $S = 1096.89...x + 43997.4...$, or $S = 1096.89...x + 45094.3...$

Kaia's salary in 2021 is \$56063.21 (accept \$56817.09 from $b = -2.16 \times 10^6$) ***A1***

Kaia had a higher salary than Gemma in 2021 ***AG***

[3 marks]

Total [6 marks]

4. $\mathrm{P}(A \cup B) = \mathrm{P}(A) + \mathrm{P}(B) - \mathrm{P}(A \cap B) = 0.68$

substitution of $\mathrm{P}(A) \cdot \mathrm{P}(B)$ for $\mathrm{P}(A \cap B)$ in $\mathrm{P}(A \cup B)$ ***(M1)***

$\mathrm{P}(A) + \mathrm{P}(B) - \mathrm{P}(A)\mathrm{P}(B)$ $(= 0.68)$

substitution of $3\mathrm{P}(B)$ for $\mathrm{P}(A)$ ***(M1)***

$3\mathrm{P}(B) + \mathrm{P}(B) - 3\mathrm{P}(B)\mathrm{P}(B) = 0.68$ (or equivalent) ***(A1)***

Note: The first two ***M*** marks are independent of each other.

attempts to solve their quadratic equation ***(M1)***

$\mathrm{P}(B) = 0.2, 1.133... \left(\frac{1}{5}, \frac{17}{15}\right)$

$\mathrm{P}(B) = 0.2 \left(= \frac{1}{5}\right)$ ***A2***

Note: Award ***A1*** if both answers are given as final answers for $\mathrm{P}(B)$.

[6 marks]

5. (a) 0.28 (s) ***A1***

[1 mark]

(b) $\text{IQR} = 0.35 - 0.27 \ (= 0.08)$ (s) ***(A1)***

substituting **their** IQR into correct expression for upper fence ***(A1)***

$0.35 + 1.5 \times 0.08 \ (= 0.47)$ (s)

$0.46 < 0.47$ ***R1***

so 0.46 (s) is not an outlier ***AG***

[3 marks]

(c) **EITHER**

the median is closer to the lower quartile (positively skewed) ***R1***

OR

The distribution is positively skewed ***R1***

OR

the range of reaction times below the median is smaller than the range of reaction times above the median ***R1***

Note: These are sample answers from a range of acceptable correct answers. Award ***R1*** for any correct statement that explains this.

Do not award ***R1*** if there is also an incorrect statement, even if another statement in the answer is correct. Accept a correctly and clearly labelled diagram.

[1 mark]

continued…

Question 5 continued

(d) **EITHER**

the distribution for ‘not sleeping well’ is centred at a higher reaction time ***R1***

OR

The median reaction time after not sleeping well is equal to the upper quartile reaction time after sleeping well ***R1***

OR

75% of reaction times are <0.35 seconds after sleeping well, compared with 50% after not sleeping well ***R1***

OR

the sample size of 9 is too small to draw any conclusions ***R1***

Note: These are sample answers from a range of acceptable correct answers. Accept any relevant correct statement **that relates to the median and/or quartiles shown in the box plots**. **Do not accept** a comparison of means. Do not award ***R1*** if there is also an incorrect statement, even if another statement in the answer is correct.
Award ***R0*** to “correlation does not imply causation”.

[1 mark]

Total [6 marks]

6. (a) recognises the need to find the value of t when $v = 0$ ***(M1)***

$t = 1.57079...\ \left(= \frac{\pi}{2}\right)$

$t = 1.57\ \left(= \frac{\pi}{2}\right)$ (s) ***A1***

[2 marks]

(b) recognises that $a(t) = v'(t)$ ***(M1)***

$t_1 = 2.26277...$, $t_2 = 2.95736...$

$t_1 = 2.26$, $t_2 = 2.96$ (s) ***A1A1***

Note: Award ***M1A1A0*** if the two correct answers are given with additional values outside $0 \le t \le 3$.

[3 marks]

(c) speed is greatest at $t = 3$ ***(A1)***

$a = -1.83778...$

$a = -1.84$ (m s^{-2}) ***A1***

[2 marks]

Total [7 marks]

Section B

7. (a) $A\hat{B}C = 27°$ ***(A1)***

attempt to substitute into cosine rule ***(M1)***

$175^2 + 230^2 - 2(175)(230)\cos 27°$ ***(A1)***

$108.62308\ldots$

$AC = 109\ (\text{m})$ ***A1***

[4 marks]

(b) correct substitution into area formula ***(A1)***

$\frac{1}{2} \times 175 \times 230 \times \sin 27°$

$9136.55...$

$\text{area} = 9140\left(\text{m}^2\right)$ ***A1***

[2 marks]

(c) attempt to substitute into sine rule or cosine rule ***(M1)***

$\frac{\sin 27°}{108.623...} = \frac{\sin \hat{A}}{175}$ OR $\cos A = \frac{(108.623...)^2 + 230^2 - 175^2}{2 \times 108.623... \times 230}$ ***(A1)***

$47.0049\ldots$

$C\hat{A}B = 47.0°$ ***A1***

[3 marks]

continued…

Question 7 continued

(d) **METHOD 1**

recognizing that for areas to be equal, $\mathrm{AD}=\mathrm{DC}$ ***(M1)***

$\mathrm{AD}=\frac{1}{2}\mathrm{AC}=54.3115...$ ***A1***

attempt to substitute into cosine rule to find BD ***(M1)***

correct substitution into cosine rule ***(A1)***

$\mathrm{BD}^2=230^2+54.3115^2-2(230)(54.3115)\cos 47.0049°$

$\mathrm{BD}=197.009...$

$\mathrm{BD}=197(\mathrm{m})$ ***A1***

[5 marks]

continued…

Question 7 continued

METHOD 2

correct expressions for areas of triangle BDA and triangle BCD using BD ***A1***

$\frac{1}{2}\times \mathrm{BD}\times 230\times \sin x°$ and $\frac{1}{2}\times \mathrm{BD}\times 175\times \sin(27-x)°$ OR

$\frac{1}{2}\times \mathrm{BD}\times 230\times \sin(27-x)°$ and $\frac{1}{2}\times \mathrm{BD}\times 175\times \sin x°$

correct equation in terms of x ***(A1)***

$175\sin(27-x)=230\sin x$ or $175\sin\mathrm{x}=230\sin(27-x)$

$x=11.6326...$ or $x=15.3673...$ ***(A1)***

substituting their value of x into equation to solve for BD ***(M1)***

$\frac{1}{2}\times \mathrm{BD}\times 230\times \sin 11.6326...=\frac{1}{2}\times \mathrm{BD}\times 175\times \sin 15.3673...$ or

$\frac{1}{2}\times \mathrm{BD}\times 230\times \sin 11.6326...=\frac{1}{2}\times 9136.55...$

$\mathrm{BD}=197(\mathrm{m})$ ***A1***

[5 marks]

Total [14 marks]

8. (a) (i) 32 (cm) ***A1***

(ii) $h_A(0) = \sin(6) + 27$ ***(M1)***

$= 26.7205...$

$= 26.7$ (cm) ***A1***

[3 marks]

(b) attempts to solve $h_A(t) = h_B(t)$ for t ***(M1)***

$t = 4.00746..., 4.70343..., 5.88332...$

$t = 4.01, 4.70, 5.88$ (weeks) ***A2***

[3 marks]

continued…

Question 8 continued

(c) recognises that $h_A'(t)$ and $h_B'(t)$ are required ***(M1)***

attempts to solve $h_A'(t) = h_B'(t)$ for t ***(M1)***

$t = 1.18879...$ and $2.23598...$ OR $4.33038...$ and $5.37758...$ OR $7.47197...$ and $8.51917...$ ***(A1)***

Note: Award full marks for $t = \frac{4\pi}{3} - 3, \frac{5\pi}{3} - 3, \left(\frac{7\pi}{3} - 3, \frac{8\pi}{3} - 3, \frac{10\pi}{3} - 3, \frac{11\pi}{3} - 3\right)$.
Award subsequent marks for correct use of these exact values.

$1.18879... < t < 2.23598...$ OR $4.33038... < t < 5.37758...$ OR
$7.47197... < t < 8.51917...$ ***(A1)***

attempts to calculate the total amount of time ***(M1)***

$3(2.2359... - 1.1887...)$ $\left(= 3\left(\left(\frac{5\pi}{3} - 3\right) - \left(\frac{4\pi}{3} - 3\right)\right)\right)$

$= 3.14$ $(= \pi)$ (weeks) ***A1***

[6 marks]

Total [12 marks]

9. (a) **METHOD 1**

$T \sim \mathrm{N}(35, \sigma^2)$

$\mathrm{P}(T > 40) = 0.25$ or $\mathrm{P}(T < 40) = 0.75$ ***(M1)***

attempt to solve for σ graphically or numerically using the GDC ***(M1)***

graph of normal curve $T \sim \mathrm{N}(35, \sigma^2)$ for $\mathrm{P}(T > 40)$ and $y = 0.25$ OR $\mathrm{P}(T < 40)$ and $y = 0.75$ OR table of values for $\mathrm{P}(T < 40)$ or $\mathrm{P}(T > 40)$

$\sigma = 7.413011...$

$\sigma = 7.41$ (min) ***A2***

METHOD 2

$T \sim \mathrm{N}(35, \sigma^2)$

$\mathrm{P}(T > 40) = 0.25$ or $\mathrm{P}(T < 40) = 0.75$ ***(M1)***

$z = 0.674489...$ ***(A1)***

valid equation using their z-score (clearly identified as z-score and not a probability) ***(M1)***

$\frac{40-35}{\sigma} = 0.674489...$ OR $5 = 0.674489...\sigma$

$7.413011\ldots$

$\sigma = 7.41$ (min) ***A1***

[4 marks]

(b) $\mathrm{P}(T > 45)$ ***(M1)***

$= 0.0886718...$

$= 0.0887$ ***A1***

[2 marks]

continued…

Question 9 continued

(c) recognizing binomial probability ***(M1)***

$L \sim \mathrm{B}(5, 0.0886718...)$

$\mathrm{P}(L \geq 1) = 1 - \mathrm{P}(L = 0)$ OR

$\mathrm{P}(L \geq 1) = \mathrm{P}(L = 1) + \mathrm{P}(L = 2) + \mathrm{P}(L = 3) + \mathrm{P}(L = 4) + \mathrm{P}(L = 5)$ ***(M1)***

$0.371400\ldots$

$\mathrm{P}(L \geq 1) = 0.371$ ***A1***

[3 marks]

(d) recognizing conditional probability in context ***(M1)***

finding $\{L < 3\} \cap \{L \geq 1\} = \{L = 1, L = 2\}$ (may be seen in conditional probability) ***(A1)***

$\mathrm{P}(L = 1) + \mathrm{P}(L = 2) = 0.36532...$ (may be seen in conditional probability) ***(A1)***

$\mathrm{P}(L < 3 \mid L \geq 1) = \dfrac{0.36532...}{0.37140...}$ ***(A1)***

$0.983636\ldots$

0.984 ***A1***

[5 marks]

continued…

Question 9 continued

(e) **METHOD 1**

recognizing that Suzi can be late no more than once (in the remaining six days) ***(M1)***

$\mathrm{X} \sim \mathrm{B}(6,\ 0.0886718...)$, where X is the number of days late ***(A1)***

$\mathrm{P}(X \le 1) = \mathrm{P}(X = 0) + \mathrm{P}(X = 1)$ ***(M1)***

$= 0.907294...$

$\mathrm{P}(\text{Suzi gets a bonus}) = 0.907$ ***A1***

Note: The first two marks may be awarded independently.

METHOD 2

recognizing that Suzi must be on time at least five times (of the remaining six days) ***(M1)***

$\mathrm{X} \sim \mathrm{B}(6,\ 0.911328...)$, where X is the number of days on time ***(A1)***

$\mathrm{P}(X \ge 5) = 1 - \mathrm{P}(X \le 4)$ OR $1 - 0.0927052...$ OR $\mathrm{P}(X = 5) + (X = 6)$ OR $0.334434... + 0.572860...$ ***(M1)***

$= 0.907294...$

$\mathrm{P}(\text{Suzi gets a bonus}) = 0.907$ ***A1***

Note: The first two marks may be awarded independently.

[4 marks]

Total [18 marks]